# 9 Nanoholes array and polarization effect

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$$p = \alpha_E (E_z^{\text{ext}} + G_{zz}p - Hm) + \alpha'_E (G_{zz}p' - Hm'),$$

$$p' = \alpha'_E (E_z^{\text{ext}} + G_{zz}p - Hm) + \alpha_E (G_{zz}p' - Hm'),$$

$$m = \alpha_M (H_y^{\text{ext}} + G_{yy}m - Hp) + \alpha'_M (G_{yy}m' - Hp'),$$

$$m' = \alpha'_M (H_y^{\text{ext}} + G_{yy}m - Hp) + \alpha_M (G_{yy}m' - Hp'),$$

with a new lattice sum defined as

$$H = -ik\sum_{n\neq 0} e^{-ik_{\parallel}x_n} \partial_{x_n} \frac{e^{ikR_n}}{R_n}.$$

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FIG. 1. Scanning electron micrographs of square nanohole arrays in gold. (a) Nearly circular holes. (b) Elliptical holes, 0.6 aspect ratio and major axis at  $-12^{\circ}$  to the [1, 0]. (c) Elliptical holes, 0.6 aspect ratio and major axis at 33° to the [1, 0] axis. (d) An expanded view of (c) showing the full 16.1  $\mu$ m wide array of 529 holes (holes spaced by 704 nm).



FIG. 2. Transmission spectrum through elliptical nanohole array for two orthogonal linear polarizations, with a 0.3 aspect ratio between the minor and major axes of the ellipse. The p polarization is parallel to the [0, 1] direction.



FIG. 3. Polarization dependence of transmission at the (0, 1) resonance peak, normalized to the maximum. Transmission shows cosine dependence when the major axis of the ellipse is oriented both at 0° and 33° to the [1, 0] axis of the array. The *p* polarization, along the [0, 1] direction of the lattice, corresponds to a polarization angle of zero degrees. The maximum transmission occurs for polarization perpendicular to the broad side of the ellipse.



FIG. 4. The depolarization ratio of the transmitted light as a function of the aspect ratio of the holes. Solid line shows the  $y = x^2$  curve.



FIG. 5. (a) Elliptical holes approaching limiting case of slits, which only show enhanced transmission for p polarized light. (b) Enhanced SP excitation perpendicular to major axis of ellipse leads to preferential excitation of the (0, 1) resonance with respect to the (1, 0) resonance. (c) Coupling both into and out of the SP mode is required to obtain enhanced transmission from periodic array of holes, which results in a squared dependence of the enhanced transmission on the coupling strength.



30°

•

•1 µm•

b

$$\lambda^{\text{SP}}(i,j) = p\left(i^2 + j^2\right)^{-1/2} \left(\frac{\varepsilon_d \varepsilon_m}{\varepsilon_d + \varepsilon_m}\right)^{1/2}$$

where the wavelength for coupling  $(\lambda^{SP})$  is governed by the periodicity p of the array,  $\varepsilon_d$  is the relative permittivity of the dielectric,  $\varepsilon_m$  is the dielectric constant of the metal, and i and j are integers related to the scattering order of the grating.





a bare gold surface; b gold with monolayer of MUA; and c gold-MUA layer with BSA.

#### **Polarization dependent of biaxial nanoholes**



(a) Shown is a schematic diagram of the SPP imaging system. The array illumination is from a laser of wavelength  $\lambda$  0 focused with a microscope objective. The resulting SPP mode is imaged on a CCD array using a 4F imaging system (MO and Lens). For the case shown, the incident  $+45^{\circ}$ polarization is decomposed into orthogonal components that excite (1,0) modes at the array, which radiate in the forward and backward directions. The radiation is polarized at  $-45^{\circ}$  to obtain the field in the image plane. MO1, MO2: Microscope objectives.  $\Psi P$ ,  $\Psi A$ : Polarizer, analyzer angles. (b) Shown are spectral measurements of unpolarized zero-order transmittance for hole arrays in an aluminum film on a glass substrate. Data from arrays with different periods, a, were combined for the composite intensity image. The stitching frequencies appear as horizontal black lines, and data are replicated at negative wavenumbers for viewing. The SPP images correspond to four values of a/  $\lambda$  0. The polarizer-analyzer pair was arranged at  $0^{\circ}$  /90° degrees for the ( $\pm$ 1,  $\pm$ 1) modes of the nanohole array 1.03 with  $a/\lambda 0 = 1.41$ , and  $at +45^{\circ}/-45^{\circ}$  for the  $(\pm 1,0)$  and  $(0,\pm 1)$  modes for  $a/\lambda 0 =$ 1.03. Higher order modes were obtained at a/ $\lambda$  0 = 2. No SPP excitation is observed for  $a/\lambda 0 = 0.9$ .





(a) Shown is a diagram of a 2D nanoholearray-based sensor. The input and output polarization states of a tunable laser are controlled, providing variable spectral or angular Fano-type profiles. A microfludic channel transports the analyte fluid to the surface of the sensing area, and can tune SPP frequency the resonance bv controlling the refractive index at the metaldielectric interface. Shown in the upper left are scanning electron microscope images of (b) representative sample. The а resonance-peak position shift is plotted versus the fluidic over-layer refractive index change, which depends on salt concentration. The black line is a linear fit to the log-log data.  $\triangle$  n: Refractive index change.  $\theta$  : Resonant phase peak shift.

#### **On-chip integration and application of nanoholes array**



#### **Optical trapping with nanoholes**

#### Manipulation target:

- > cells, virus, DNA
- > non-biological particles in fluidic

#### Critical trapping distance from the surface, d

$$d = \frac{\lambda}{4\pi} \sqrt{\frac{n_m^2 + \varepsilon_m}{-n_m^4}} \ln\left(\frac{3\lambda^3}{16\pi^3 a^3} \frac{n_m}{\sqrt{-(n_m^2 + \varepsilon_m)}} \frac{m^2 + 2I_x(0)}{m^2 - 1}\right)$$



The polarization induced on the gold nanoparticle by a local electric field can then be written as

$$\boldsymbol{p}(\boldsymbol{r}) = \begin{pmatrix} \alpha_x & 0\\ 0 & \alpha_z \end{pmatrix} \boldsymbol{E}(\boldsymbol{r}) \tag{1}$$

Here, x and z are the polarizabilities along the x and z axes, respectively. In the data shown in Fig. 1b, z/x is 1.18 at a wavelength of 780 nm, implying that the attached gold nanoparticle is slightly elliptical in shape



For an evanescent standing wave, generated by two counter-propagating *p*-polarized beams of equal intensity, the field vector is given by

$$E(\mathbf{r}) = (E_x, 0, E_z) = E_0 \left(\cos kx, 0, -\frac{k}{\kappa}\sin kx\right) e^{-\kappa z}$$
(2)

where  $E_0$  is a constant magnitude, *k* and are related by the Helmholtz equation,  $k^2 = (\omega/c)^2$ , and are determined by the angle of incidence and the index of refraction of the prism.

The electric field of this standing wave can be written in the same form as equation (2), but now with a much larger k/ ratio equal to (-m) where m is the dielectric constant of gold:

$$E(r) = (E_x, 0, E_z) = E_0(\cos kx, 0, -\sqrt{-\varepsilon_m} \sin kx)e^{-\kappa z}$$
 (3)

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Figure 2: Vector-field mapping of the surface-plasmon polariton standing wave



a, An SEM image of the single slit, showing the asymmetric slit shape. **b**, Constant-height scan image at z = 100 nm, rotating the polarizer by  $360^{\circ}$  . **c**, Vector-field image of a 3 m 2 m starting from area z = 100 nm, together the total electric with field intensity plot on a blue-red colour scale. At the bottom is shown an atomic force microscopic image of the slit profile. **d**, An FDTD calculation assuming an asymmetric trapezoidal slit shape. e, Experimental |Ez|2plotted on a (different) blue-red colour scale. f, Theoretical |*Ez*|2 profile.

Figure 3: Vector-field mapping of light emerging from a single slit.



where  $\lambda$  is the wavelength of the light source,  $n_m$  is the refractive index of the medium in which the particles are suspended,  $\varepsilon_m$  is the real part of the dielectric constant of the metal, a is the particle radius,  $m = \frac{n_p}{n_m}$  is the refractive index contrast, with  $n_p$  being the refractive index of the particle,  $I_{x}(0)$  is the surface plasmon intensity at the surface of the metal, and  $I_{\tau}$  is the intensity of the transmitted light through the nanoholes. If the surface plasmon intensity is slightly higher than the transmitted light intensity, a trapping distance of 0.5 µm may be obtained

## Practical plasmonic crystal biosensors

Images and schematic illustrations of a quasi-3D plasmonic crystal. (A) Scanning electron micrograph (SEM) of a crystal. (Upper Inset) A low-resolution optical image illustrating the diffraction colors produced by these structures. (Lower Inset) A high-magnification SEM that shows the upper and lower levels of gold. (B) Schematic illustration of the normal incidence transmission mode geometry used to probe these devices. The intensity of the undiffracted, transmitted light is monitored across the UV, visible, and near-infrared regions of the spectrum. (Inset) A close-up schematic illustration of the crystal.



A hybrid plasmonic-photonic nanodevice for label-free detection of a few molecules







Fluorescence image of target DNA labeled with Cy-5 hybridized to the probe DNA immobilized within the nanostructured patterns by means of electron beam lithography onto organosilane self-assembled monolayer resist (Size:250nm, Pitch:2.5µm).



Fluorescence images of single GroEL enzymes labeled with IC-5 immobilized in the metal nanohole array on a quartz glass substrate. The quantized photo-bleaching proves the single molecule detection in each nanohole. The fluorescent dye Cy-5, which is diffused in water so that it mimics a protein in order to interact with GroEL, does not produce background noises because the laser light is guided only to the immobilized GroEL via the nanohole wave-guides.